Oneness-Family School - Sixth - Eighth Grade - Math Benchmarks Academy: Math

## MATH

| Introduction to Pre-Algebra | Pre-Algebra | Algebra | Geometry |
| :---: | :---: | :---: | :---: |
| Can analyze problems by identifying relations, distinguishing relevant from irrelevant information, and identifying missing information <br> Can write and solve one-step linear equations in one variable <br> Can solve problems using the correct order of operations <br> Can apply algebraic order of operations and properties and justify each step in a process <br> Can use a variety of methods to explain mathematical reasoning <br> Can compare and order positive and negative fraction, decimals, and mixed numbers and place them on a number line <br> Can use graphs to explain mathematical reasoning <br> Can solve addition, subtraction, multiplication, and division problems, including that use positive and negative integers and combinations of these operations | Can use variables, expression, and equations to model real-world problems <br> Can predict, find, and justify solutions to application problems using appropriate tables, graphs and algebraic equations <br> Can locate and name points on a coordinate graph <br> Can draw conclusions and make predictions using scatter plots <br> Can compare and order integers <br> Can select appropriate operations to solve problems involving integers <br> Can locate and name points on a coordinate plane using ordered pairs of integers <br> Can graph reflections and translations on a coordinate plane <br> Can explore rational numbers | Can translate between mathematical and verbal expressions and equations <br> Can evaluate numerical and algebraic expressions using the order of operations <br> Can solve open sentence equations and inequalities <br> Can recognize and use the properties of identity and equality. <br> Can use the Distributive Property to simplify and evaluate expressions. <br> Can recognize and use the Commutative and Associative Properties to simplify algebraic expressions <br> Can identify the hypothesis and conclusion in a conditional statement <br> Can use a counterexample to show that an assertion is false <br> Can classify and graph real numbers <br> Can find square roots and order real numbers | Can identify and model points, lines, and planes <br> Can identify collinear and coplanar points and intersecting lines and planes in space <br> Can measure segments, determine accuracy of measurement, and compute with measures <br> Can find the midpoint of a segment and the distance between points <br> Can identify and use congruent angles and the bisector of an angle <br> Can identify and name polygons and find perimeters of polygons <br> Can make conjectures based on inductive reasoning and find counterexamples <br> Can determine truth values of conjunctions and disjunctions and construct truth tables <br> Can analyze statements in if-then form and write the converse, inverse, and contrapositive of if-then statements <br> Can use the Law of Detachment and the Law of Syllogism <br> Can identify and use basic postulates about points, lines, and planes |

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Can write an algebraic expression for a given situation, using up to three variables

Can solve problems involving rates, average speed, distance, and time

Can use variables in expressions describing the formulas for the perimeter of a rectangle

Can determine the least common multiple and the greatest common divisor of whole numbers and use them to solve problems with fractions

Can compare and order positive and negative fractions, decimals, and mixed numbers and place them on a number line

Can solve problems involving addition, subtraction, multiplication, and division of positive fractions

Can explain the meaning of multiplication and division of positive fractions and perform the calculations

Can interpret and use ratios in different contexts to show the relative sizes of two quantities, using appropriate notations

Can use proportions to solve problems

Can multiply and divide fractions

Can add and subtract like fractions and unlike fractions

Can convert fractions to decimals

Can factor numbers
Can determine least common multiple

Can communicate mathematical ideas using algebraic mathematical models

Can predict, find, and justify solutions to application problems using algebraic equations

Can use formulas to solve problems

Can translate verbal phrases into inequalities

Can compare and contrast proportional and non proportional linear relationships

Can use proportional relationships in similar twodimensional figures to find missing measurements

Can draw and interpret graphs of functions

Can solve equations by using addition, subtraction, multiplication, and division

Can determine whether two ratios form a proportion
Can solve equations involving more than one operation, including equations with grouping symbols and variables on both sides

Can solve consecutive integer problems

Can solve proportions
Can find percents of increase and decrease

Can solve problems involving percents of change

Can solve equations for given variables

Can use formulas to solve real-world problems

Can solve uniform motion problems
Can solve mixture problems
Can represent relation as sets of ordered pairs, tables, mappings, and graphs

Can write paragraph proofs
Can use algebra to write two-column proofs
Can use properties of equality in geometry proofs Can write proofs involving segment addition, segment congruence, supplementary and complementary angles, and congruent and right angles

Can identify the relationships between two lines or two planes

Can name angles formed by a pair of lines and a transversal

Can use the properties of parallel lines to determine congruent angles

Can use algebra to find angle measures
Can find slopes of lines and use slope to identify parallel and perpendicular lines

Can write an equation of a line using given information and can solve problems by writing equations

Can recognize angle conditions that occur with parallel lines and prove that two lines are parallel based on given angle relationships

Can find the distance between a point and a line and the distance between parallel lines

Can identify and classify triangles by angles and sides

Can convert one unit of measure to another

Can demonstrate an understanding that rate is a measure of one quantity per unit value of another quantity

Can interpret and use ratios in different contexts
Can solve problems involving rates
Can calculate given percents of quantities

Can understand how additional data added to data sets may affect measures of central tendency

Can explain why a specific measure of central tendency provides the most useful information in a given context

Can explain how the inclusion or exclusion of outliers affects measures of central tendency

Can analyze data displays
Can identify different ways of selecting a sample and which method makes a sample more representative for a population

Can identify claims based on statistical data

Can use ratios, proportions, and percent of change to solve problems

Can evaluate a solution for reasonableness

Can select and use appropriate representations for presenting and displaying relationships among collected data

Can generate a different representation of data given another representation of data

Can predict, find, and justify solutions to application problems using appropriate tables, graphs, and algebraic equations

Can draw conclusions and make predictions by analyzing trends in scatter plots

Can examine factors and monomials

Can evaluate expressions with powers and exponents

Can multiply and divide monomials

Can find the inverse of a function
Can determine whether a relation is a function.

Can find functional values.
Can identify linear equations, intercepts, and zeros

Can graph linear equations
Can recognize arithmetic sequences and extend and write formulas for arithmetic sequences

Can write equations for proportional and non-proportional relationships

Can use rate of change to solve problems

Can find the slope of a line
Can write and graph direct variation equations

Can solve problems involving direct variation

Can write and graph linear equations in slope-intercept form

Can model real-world data with an equation in slope-intercept form

Can write an equation of a line given the slope and one point on the line

Can apply the Angle Sum Theorem and the Exterior Angle Theorem

Can name and label corresponding parts of congruent triangles and identify congruence transformations

Can uses the SSS, SAS, and ASA Postulates and the AAS Theorem to test for triangle congruence

Can use the properties of isosceles and equilateral triangles

Can position and label figures in order to write coordinate proofs and can prove theorems using coordinate proofs

Can identify and use perpendicular bisectors, and angle bisectors, medians, and altitudes in triangles

Can recognize and apply properties of inequalities to the measure of the angles of a triangle and the relationship between angles and sides of a triangle

Can apply the Triangle inequality Theorem
Can determine the shortest distance between a point and a line

Can apply the SAS and SSS Inequalities
Can identify similar figures and solve problems involving scale factors

Can use proportional parts of triangles

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Can identify data that represent sampling errors and explain why the sample might be biased

Can represent probabilities as ratios, proportions, decimals, and percentages and verify that the probabilities computed are reasonable

Can represent all possible outcomes for compound events in an organized way and express the theoretical probability of each outcome

Can identify independent and dependent events

Can calculate the probability of either of two disjoint events and the probability of one event following another

Can identify angles as vertical, adjacent, complementary, or supplementary and describe each term

Can use the properties of complementary and supplementary angles and the sum of the angles of a triangle to solve problems involving an unknown angle

Can use coordinate graphs to plot simple figures, determine lengths and areas related to them, and

Can express numbers using positive and negative exponents

Can use scientific notation
Can communicate mathematical ideas using language, efficient tools, appropriate units, and graphical, numerical, physical or algebraic mathematical models

Can predict, find, and justify solutions to application problems using appropriate tables, graphs, and algebraic equations

Can communicate mathematical ideas using algebraic mathematical models
Can use geometric concepts and properties to solve problems in fields such as art and architecture

Can use the Pythagorean Theorem to solve real-world problems

Can graph rotations on coordinate plane

Can use properties to classify quadrilaterals and other polygons

Can write an equation of a line given two points on the line

Can write the equation of a line in point-slope form

Can write linear equations in different forms

Can interpret points on a scatter plot
Can use lines of fit to make and evaluate predictions

Can write an equation of the line that passes through a given point, parallel to a given line

Can write an equation of the line that passes through a given point, perpendicular to a given line

Can determine whether a system of linear equations has no, one, or infinitely many solutions

Can solve systems of equations by graphing, using substitution, and using elimination

Can solve real-world problems involving systems of equations

Can determine the best method for solving systems of equations

Can solve linear inequalities by using addition, subtraction, multiplication and division

Can divide a segment into parts
Can recognize and use proportional relationships of corresponding perimeters, angle bisectors, altitudes, and medians of similar triangles

Can find the geometric mean of two numbers
Can solve problems involving relationships between parts of a right triangle and the altitude to its hypotenuse

Can use the Pythagorean Theorem and its converse

Can use the properties of special right triangles
Can find trigonometric ratios using right triangles and can solve problems using trigonometric ratios

Can use the Law of Sines and the Law of Cosines to solve triangles

Can solve problems using the Law of Sines and the Law of Cosines

Can find the sum of the measures of the interior and exterior angles of a polygon

Can recognize and apply properties of the sides, angles, and diagonals of parallelograms

Can recognize the conditions that ensure a quadrilateral is a parallelogram and prove that a set of points forms a parallelogram in the coordinate plane

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determine their image under translations and reflections

Can use variables in expressions describing geometric quantities

Can express, in symbolic form, simple relationships arising from geometry

Can understand the concept of a constant such as $\pi$

Can recall and use the formulas for the circumference and area of circles

Can recall and use common estimates of $\pi$ to calculate the circumference and area of circles

Can recall and use the formulas for the volume of triangular prisms and cylinders

Can determine the two integers between which the root of a non-square integer lies and explain why

Can recall and understand the Pythagorean Theorem and its converse

Can use the Pythagorean Theorem to find the length of the missing side of a right triangle and the lengths of other line segments

Can calculate areas for standard quadrilaterals, triangles and circles

Can calculate the sum of the measures of the interior angles for any regular polygon

Can use properties to define and identify angle and line relationships

Can draw three-dimensional figures from different perspectives

Can connect models of prisms, cylinders, pyramids, spheres, and cones to formulas for volume of these objects

Can estimate measurements and use formulas to solve application problems involving lateral and surface area

Can use proportional relationships in similar three-dimensional figures to find missing measurements

Can select and use an appropriate representation for presenting and displaying relationships among collected data, including line plots, line graphs, stem and leaf plots,

Can solve linear inequalities involving more than one operation

Can solve linear inequalities involving the Distributive Property

Can solve compound inequalities containing the word or/and and graph their solution sets

Can solve absolute value equations
Can graph inequalities on the coordinate plane
Can solve real-world problems involving linear inequalities

Can solve systems of inequalities by graphing

Can write expressions using exponents

Can evaluate expressions with exponents using order of operations

Can factor monomials

Can multiply and divide monomials
Can apply the product and quotient of powers properties

Can use powers to compare values
Can write expressions using positive exponents

Can recognize and apply the properties of rhombi, squares, and trapezoids

Can draw reflected images
Can recognize and draw lines and points of symmetry

Can draw translated images using coordinates and repeated reflections

Can draw rotated images using the angle of rotation

Can identify figures with rotational symmetry
Can identify regular tessellations and create tessellations with specific attributes

Can determine whether a dilations is an enlargement, reduction, or congruence transformation and determine the scale factor of a given dilation

Can identify and use the parts of circles Can solve problems involving the circumference of a circle

Can recognize major arcs, minor arcs, semicircles, and central angles and their measures

Can find arc length

Can recognize and use the relationship between arcs and chords and chords and diameters

Can find the measures of inscribed angles and the measures of angles of inscribed polygons

Can use the properties of tangents
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| Can use formulas routinely for finding the surface area of basic three-dimensional figures, including prisms | circle graphs, bar graphs, box and whisker plots, histograms, and Venn diagrams, with and without the use of technology <br> Can find the probabilities of dependent and independent events <br> Can evaluate methods of sampling to determine validity of an inference made from a set of data | Can use negative exponents to solve word and real world problems <br> Can evaluate algebraic expressions with negative exponents <br> Can express numbers in standard form and scientific notation <br> Can solve problems using scientific notation <br> Can order numbers in scientific notation <br> Can use exponent rules to simplify and evaluate algebraic expressions <br> Can identify polynomials <br> Can determine the degree of a polynomials <br> Can add and subtract polynomials <br> Can multiply polynomials by monomial and polynomials <br> Can find the prime factorization and greatest common factor of monomials <br> Can factor polynomials using the Distributive Property <br> Can factor trinomials where $A=1$ <br> Can factor trinomials where $A>1$ | Can solve problems with circumscribed polygons Can find measures of angles formed by lines intersecting inside, on, or outside a circle <br> Can find the measures of segments that intersect in the interior or exterior of a circle <br> Can write the equation of a circle <br> Can find the perimeters and areas of parallelograms, triangles, rhombi, circles, regular polygons, and irregular figures <br> Can solve problems involving geometric probability <br> Can solve problems involving sectors and segments of circles <br> Can use orthogonal drawings of three-dimensional figures to make models <br> Can identify and use three-dimensional figures <br> Can draw two-dimensional models for three-dimensional figures <br> Can find the surface areas and lateral areas of prisms, cylinders, regular pyramids, and cones <br> Can recognize and define the basic properties of spheres <br> Can find the surface area of spheres <br> Can find volumes of prisms, cylinders, pyramids, circular cones, and spheres <br> Can solve problems involving volumes of spheres |
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|  |  |  | $\begin{array}{l}\text { Can factor the difference of squares } \\ \text { Can factor perfect squares } \\ \text { Can solve a quadratic function by } \\ \text { graphing, completing the square, or } \\ \text { using the quadratic formula } \\ \text { Can graph exponential functions }\end{array}$ |
|  Can identify congruent or similar solids  |  |  |  |
|  Can solve problems involving  |  |  |  |
|  exponential functions  |  |  |  | <br>

Case the Distance and Midpoint Formulae for <br>

points in space\end{array}$]$|  |
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